## Unified Engineering Problem Set Week 7 Fall, 2007

M7.1 (5 *points*) Write out the following tensor equations in full. *Show all appropriate steps*.

(Note: these equations do not necessarily have any real meaning)

- (a)  $C_{mn} = R_{mnjk} \gamma_j z_k$  (for m = 1, n = 3)
- (b)  $E = 1/2 \sigma_{\alpha\beta} \epsilon_{\alpha\beta}$
- (c)  $H_i = b_{\alpha\beta} P_{\alpha\beta} n_i$
- (d)  $\sigma_{31} = \ell_{3m'} \ell_{1n'} \sigma'_{m'n'}$

(e) 
$$f_{pq} \left( \frac{\partial g_q}{\partial t} \right) + x_p = 0$$

**M7.2 (5** *points)* Write out the succinct tensor equation that describes the following notation. Clearly explain all steps in arriving at the equation.

$$\begin{cases} \mathsf{M}_{1} \\ \mathsf{M}_{2} \\ \mathsf{M}_{3} \end{cases} = \begin{bmatrix} \alpha_{111} & \alpha_{221} & 2\alpha_{121} \\ \alpha_{112} & \alpha_{222} & 2\alpha_{122} \\ \alpha_{113} & \alpha_{223} & 2\alpha_{123} \end{bmatrix} \begin{cases} \mathsf{T}_{11} \\ \mathsf{T}_{22} \\ \mathsf{T}_{12} \end{cases}$$

**M7.3** (10 *points*) A second axis system is defined by rotating the  $x_1 - x_2$  plane by an angle  $\phi$  of  $-25^{\circ}$  about the  $x_3$  axis. A position vector,  $\underline{r}$ , is described in the original axis system as (NOTE: The vector is unitless):

$$\underline{\mathbf{r}} = 4\underline{\mathbf{i}}_1 - 3\underline{\mathbf{i}}_2 - 5\underline{\mathbf{i}}_3$$

- (a) Determine the expression for the vector in the rotated coordinate system.
- (b) Prove, by some means, that these two expressions are equivalent.